

Chapter 8.2 Factoring Out the GCF; Factoring by Grouping

Factoring expressions of the form $ax^2 + bx + c$ when a, b, and c have a common factor.

1. Find the GCF of a, b, and c
2. Check your answer by using the Distributive Property

Example:

Factor $12x^3 + 15x^2 - 21x$ The GCF is $3x$

$$12x^3 + 15x^2 - 21x = \boxed{3x(4x^2 + 5x - 7)}$$

To factor a polynomial with four terms use the Grouping method.

Example 1:

Factor $8x^2(x - 4) + 5(x - 4)$

$$\begin{aligned} &8x^2(x - 4) + 5(x - 4) && \text{Factor out the common factor } (x - 4) \\ &\boxed{(x - 4)(8x^2 + 5)} \end{aligned}$$

Example 2:

Factor $5x^3 + 15x^2 - 4x - 12$

$$\underbrace{5x^3 + 15x^2} - \underbrace{4x - 12} \quad \text{Group the first two terms and the last two terms}$$

$$5x^2(x + 3) - 4(x + 3) \quad \text{Factor out } 5x^2 \text{ from the first 2 terms and } -4 \text{ from the last 2 terms}$$

$$\boxed{(x + 3)(5x^2 - 4)} \quad \text{Factor out } (x + 3)$$