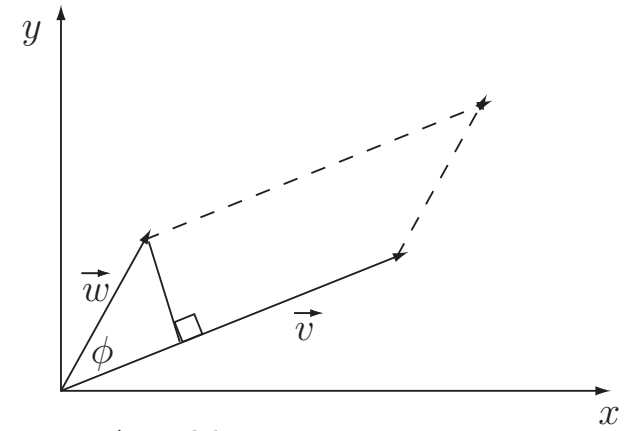


Area

For $\vec{v} = (v_1, v_2)$ and $\vec{w} = (w_1, w_2)$ there are a number of notable consequences of the relationship

$$\|\vec{v} \times \vec{w}\| = \begin{vmatrix} v_1 & v_2 \\ w_1 & w_2 \end{vmatrix} = \|\vec{v}\| \|\vec{w}\| \sin \phi$$



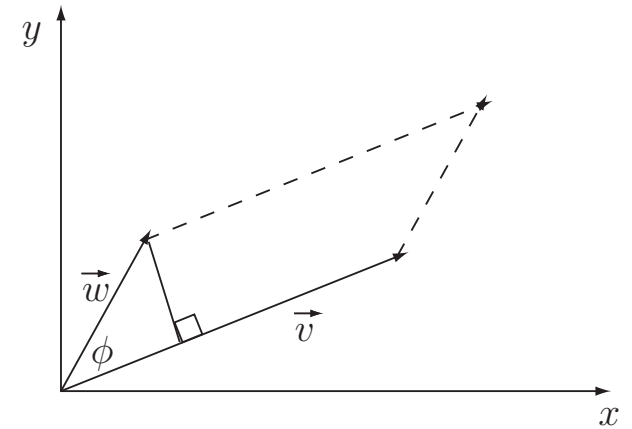
$$A = bh$$

$$= \|\vec{v}\| \|\vec{w}\| \sin(\phi)$$

Area

For $\vec{v} = (v_1, v_2)$ and $\vec{w} = (w_1, w_2)$ there are a number of notable consequences of the relationship

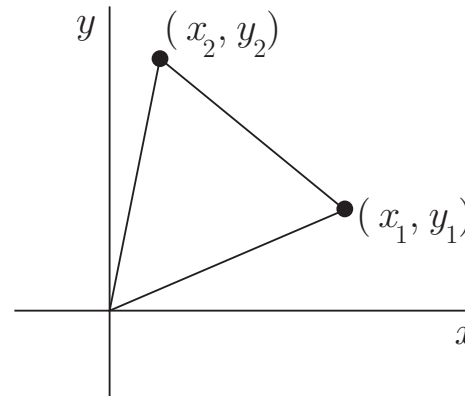
$$\|\vec{v} \times \vec{w}\| = \begin{vmatrix} v_1 & v_2 \\ w_1 & w_2 \end{vmatrix} = \|\vec{v}\| \|\vec{w}\| \sin \phi$$



$$\begin{aligned} A &= bh \\ &= \|\vec{v}\| \|\vec{w}\| \sin(\phi) \end{aligned}$$

Consider triangular area:

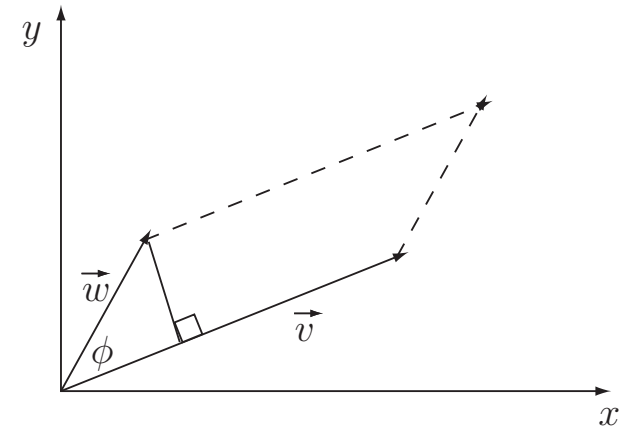
How is the result above useful here?



Area

For $\vec{v} = (v_1, v_2)$ and $\vec{w} = (w_1, w_2)$ there are a number of notable consequences of the relationship

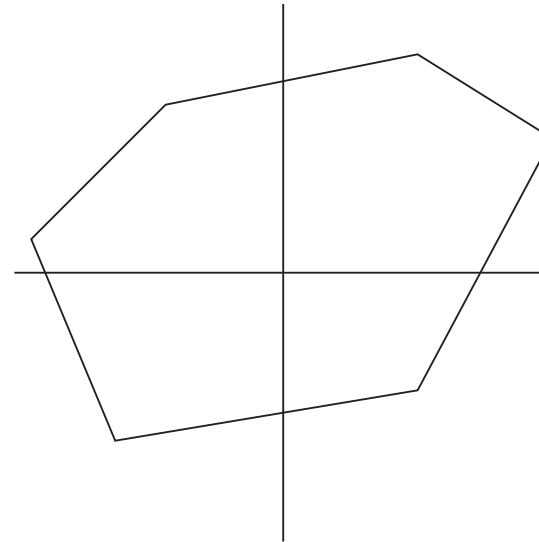
$$\|\vec{v} \times \vec{w}\| = \begin{vmatrix} v_1 & v_2 \\ w_1 & w_2 \end{vmatrix} = \|\vec{v}\| \|\vec{w}\| \sin \phi$$



$$A = bh$$

$$= \|\vec{v}\| \|\vec{w}\| \sin(\phi)$$

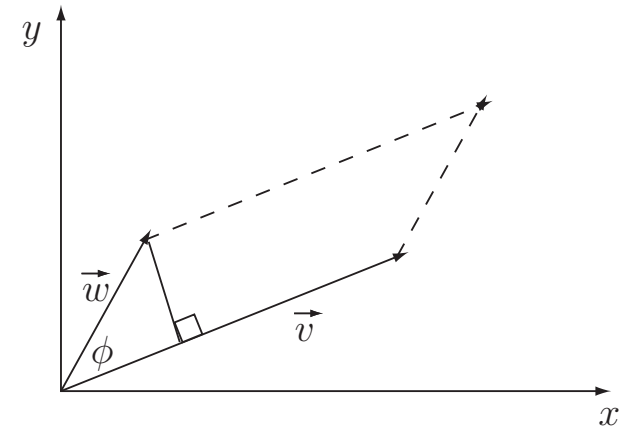
Or here?



Area

For $\vec{v} = (v_1, v_2)$ and $\vec{w} = (w_1, w_2)$ there are a number of notable consequences of the relationship

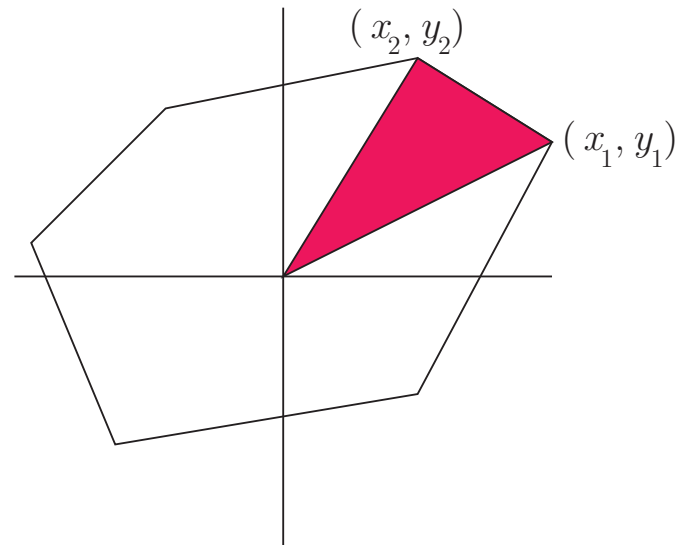
$$\|\vec{v} \times \vec{w}\| = \begin{vmatrix} v_1 & v_2 \\ w_1 & w_2 \end{vmatrix} = \|\vec{v}\| \|\vec{w}\| \sin \phi$$



$$A = bh$$

$$= \|\vec{v}\| \|\vec{w}\| \sin(\phi)$$

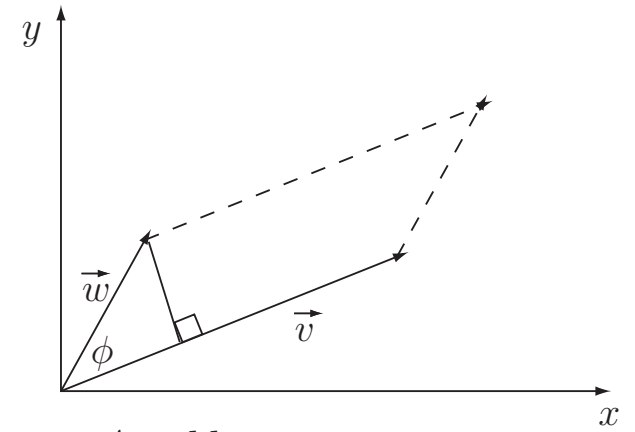
Or here?



Area

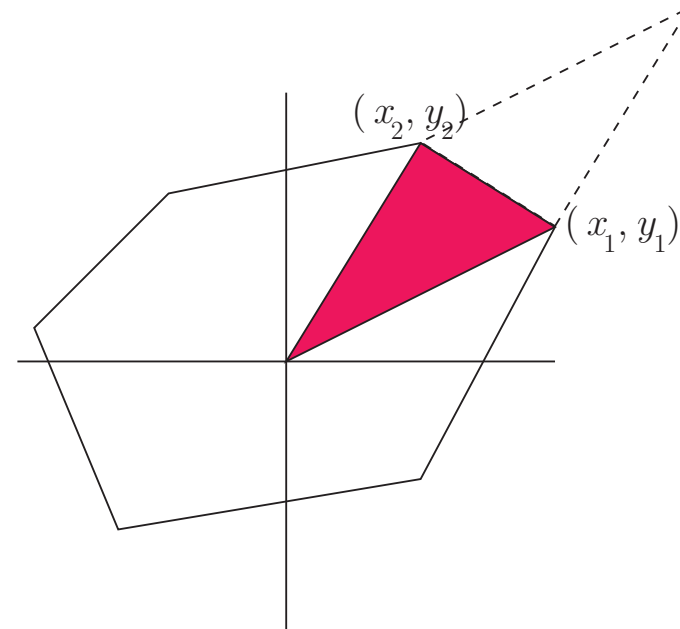
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$$\begin{aligned} A &= bh \\ &= \|\vec{v}\| \|\vec{w}\| \sin(\phi) \end{aligned}$$

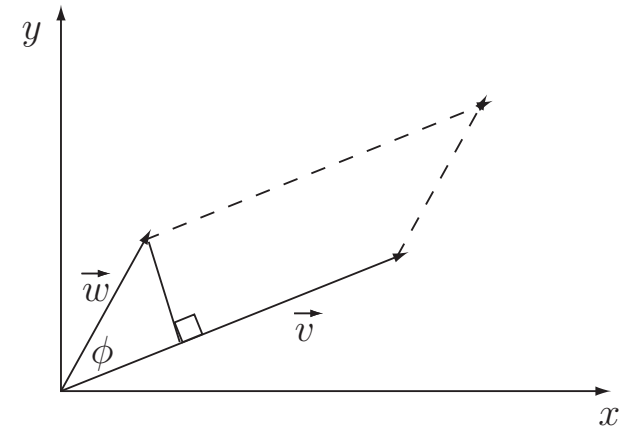
Or here?



Area

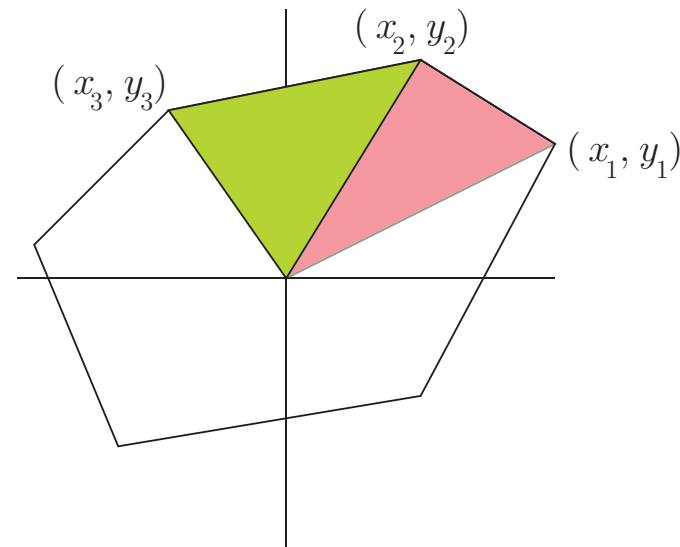
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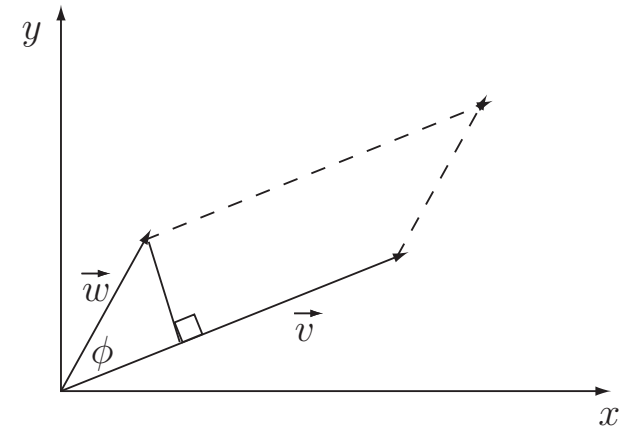
Or here?



Area

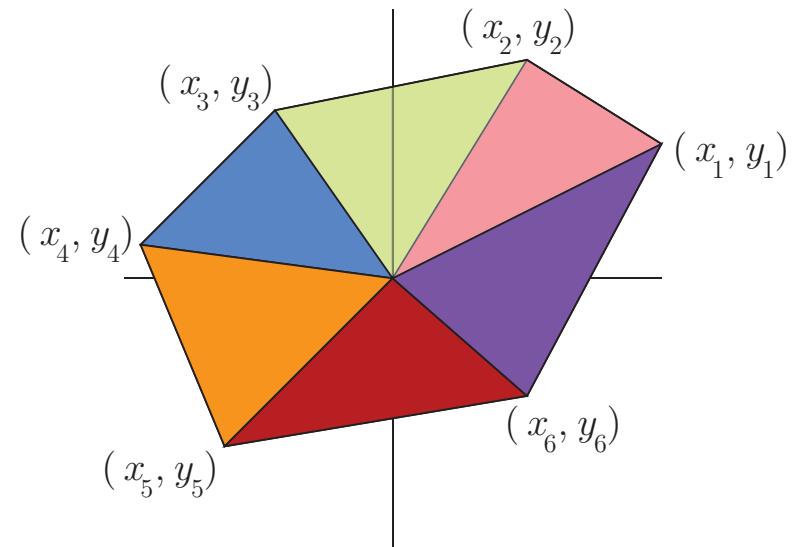
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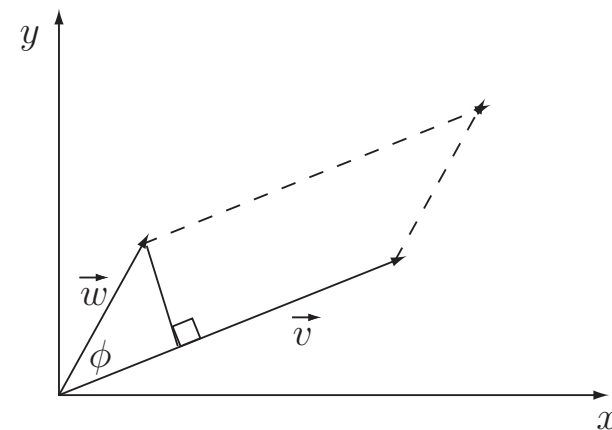
Or here?



Area

For $\vec{v} = (v_1, v_2)$ and $\vec{w} = (w_1, w_2)$ there are a number of notable consequences of the relationship

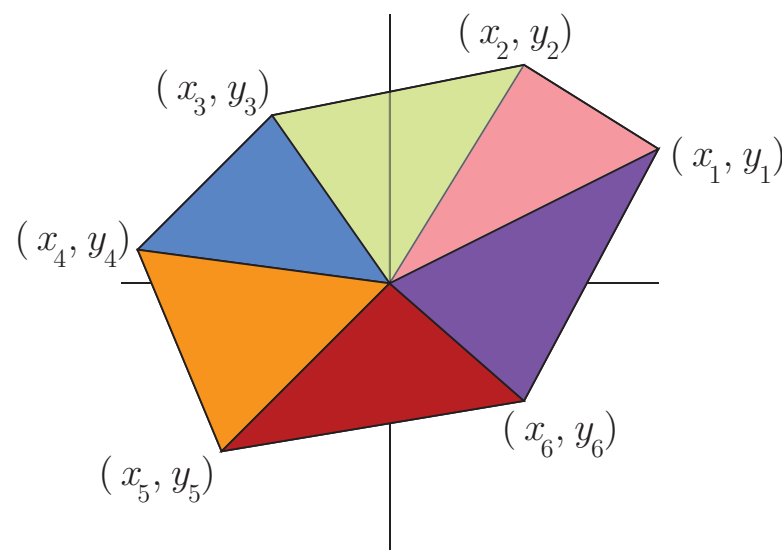
$$\|\vec{v} \times \vec{w}\| = \begin{vmatrix} v_1 & v_2 \\ w_1 & w_2 \end{vmatrix} = \|\vec{v}\| \|\vec{w}\| \sin \phi$$



$$\begin{aligned} A &= bh \\ &= \|\vec{v}\| \|\vec{w}\| \sin(\phi) \end{aligned}$$

Can you show that in general

$$A = \frac{1}{2} \left[\begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \end{vmatrix} + \begin{vmatrix} x_2 & y_2 \\ x_3 & y_3 \end{vmatrix} + \dots + \begin{vmatrix} x_n & y_n \\ x_1 & y_1 \end{vmatrix} \right]$$



Area

The formula for find the area of a polygon given the coordinates of its vertices,

$$A = \frac{1}{2} \left[\begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \end{vmatrix} + \begin{vmatrix} x_2 & y_2 \\ x_3 & y_3 \end{vmatrix} + \cdots + \begin{vmatrix} x_n & y_n \\ x_1 & y_1 \end{vmatrix} \right]$$

is often called the Surveyor's Algorithm, Gauss's Area Formula (of course), or The Shoestring Formula. It can also be evaluated like this:

$$A = \frac{1}{2} [-y_1x_2 - y_2x_3 - y_3x_4 - \cdots - y_{n-1}x_n - y_nx_1 + x_ny_1 + x_{n-1}y_n + \cdots + x_2y_3 + x_1y_2]$$